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Numerical simulation of the type inversion in n+-p-p+ Si solar cells, used for space applications, under 1 MeV electron irradiation

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Abstract

Solar cells, used for space applications, are exposed to energetic particles such as protons and electrons. The energetic particles create defects in the active region of the solar cell and the latter performance can be severely degraded. One of the phenomena observed in Silicon solar cells exposed to 1 MeV electron irradiation is type inversion of its active region. This behaviour is numerically simulated using the SCAPS software. The current-voltage characteristics of a Si n+-p-p+ structure are calculated under AM0 for different fluences of 1 MeV electrons. It was found that, amongst the many defects created, only one of them is responsible for type inversion. It is a minority trap that is an electron trap in the p-type base of the n+-p-p+ solar cell.

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1. Introduction

For terrestrial applications photovoltaic energy is still battling to find a leading place due to its relative high cost compared to other sources. However it is the only choice for space applications. Although there is a wide choice of potential materials that can be used to make solar cells, those used to power space vehicles and satellites are required to be highly efficient as well as resistant to energetic particles. The choice then becomes limited to a few materials such as Si and some III-V semiconductors and their all alloys (GaAs, InP and GaInP) [1, 2]. This is mainly due to their mature technology to produce good quality crystals with well controlled doping. Although solar cells made of compound semiconductors have higher conversion efficiencies and radiation-resistance than silicon solar cells, the

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latter have a better cost effectiveness and reliability. The solar cells used in space are subjected to charged particles. The main particles in this environment are protons and electrons of a wide energy range. These interactions introduce defects in the semiconductor lattice and, consequently, deteriorate the solar cell performance [3]. The degradation of solar cells by energetic electrons and protons in laboratories is well documented (see, for example, references [4-8]). In addition to experimental characterisation, analytical modelling is also carried out [9 -13]. The main goal of this modelling is to predict the effect of the long term exposure of the solar cells to high energetic electrons and protons [14, 15]. In this modelling the space solar figures of merit (the short circuit current $I_{SC}$, the open circuit voltage $V_{OC}$, the maximum output power $P_{MAX}$ , the fill factor $FF$ and the conversion efficiency $\eta$) decreases linearly with the logarithm of the fluence. For example, $P_{MAX}$ is related to the irradiation fluence by a simple formula of the form [16]:

$$P_{MAX}(\varphi) = P_0 \left( 1 - C \ln \frac{\varphi}{\varphi_0} \right)$$

(1)

where $\varphi$ is the irradiation fluence, $\varphi_0$ is the fluence threshold for the power reduction, $P_0$ is the pre-irradiated maximum output power and $C$ is a fitting constant. The other figures of merit follow a similar pattern. This analytical modelling is based on the fact that irradiation introduces defects which manifest as energy levels in the semiconductor energy gap and whose concentration is proportional to the fluence, thus:

$$N_i = k_i \varphi$$

(2)

The subscript $i$ denotes the $i^{th}$ defect and $k_i$ is introduction rate of the $i^{th}$ defect. It follows that the minority carrier lifetime is reduced, since it is inversely proportional to the defect concentration, as:

$$\frac{1}{\tau} = \frac{1}{\tau_0} + \sum \frac{1}{\tau_i} = \frac{1}{\tau_0} + \sum \sigma_i v_{th} N_i = \frac{1}{\tau_0} + \sum \sigma_i v_{th} k_i \varphi$$

(3)

$\tau_0$ is the pre-irradiated minority carrier lifetime, $\tau_i$ is the minority carrier lifetime set by the $i^{th}$ defect, $\sigma_i$ is the capture cross section of the $i^{th}$ defect and $v_{th}$ is the thermal velocity of minority carriers.

Using (1) it is evident that the solar cell figures of merit decrease monolithically with increasing fluence. However, in some silicon solar cells, the short circuit does not strictly follow this behaviour. Instead, it follows (1) initially and at a certain fluence it increases slightly before it decreases again and sharply [2, 4, 6, 8, 12-13, 17-18]. This slight recovery of the short circuit current is usually attributed to a type inversion of the base silicon (from n to p-type or vice versa) [19]. The type inversion itself is due to the fact that irradiation introduces compensating centres which reduce the initial doping density. As a result the space charge width increases. The phenomenon itself is called carrier removal and is modeled by an analytical expression, for a p-type silicon for example, of the form [2, 13]:

$$N_{eff} = N_A - N_{CC} = R_C \varphi$$

(4)

$N_{eff}$ is the effective doping density, $N_A$ is the initial doping density (unirradiated Si), $N_{CC}$ is the compensating centre density and $R_C$ is the removal rate. A more accurate description of the removal phenomenon is described by an exponential behaviour of the reduced hole density [13], thus:

$$p_{\varphi} = p_0 \exp \left( - \frac{R_C \varphi}{p_0} \right)$$

(5)

In their detailed analytical modelling, Bourgoin and de Angelis [2] have divided this curve into four regions. Imaizumi et al [4], Yamaguchi et al [6], Yamaguchi et al [13] and Yamaguchi et al [17] have divided the short circuit current dependence on fluence curve into three regions. The first region of [2] is just for $\varphi < \varphi_0$. The other regions are similar between these references. The second region of [2] and the first of the other references is that the short circuit decreases with increasing fluence. This is explained by a decrease in the minority carrier lifetime and hence in their diffusion length. The third region of [2] and the second of the other references is that the short circuit
increases with increasing fluence. This is related to the onset of the type inversion where the space charge width increases instead of decreasing. The fourth region of [2] and the third of the other references is that the short circuit falls sharply with increasing fluence. This is explained by the increase in the base resistivity associated with the decrease in carrier concentration. Karazhanov [12] used a straight forward analytical model describing the type inversion using a free concentration compensated by a deep level to explain the increase of the short circuit current with increasing fluence. As it is well known, irradiation creates several defects in semiconductors [1-2, 17, 20-25]. Some of them are recombination centres while others are doping compensating or enhancing centres. In experiment it is very difficult to distinguish between recombination and compensation centres. In addition, analytical modelling links the observed degradation of the solar cell figures of merit to the whole defects. In this respect numerical simulation can be of great help since it can relate the degradation of each figure of merit to a particular defect [26-31]. Of particular interest to the present work, it can reveal which defect is responsible for the type inversion and the anomalous behaviour of the short circuit current in Si solar cells. To accomplish this we have used the software SCAPS (Solar Cell Capacitance Simulator) developed by M. Burgelman and co-workers at the Department of Electronics and Information Systems (ELIS) of the University of Gent, Belgium [32].

2. Simulation

The current-voltage characteristics of the solar cell are calculated using the software SCAPS. SCAPS is a Windows application program, organised in a number of panels, in which the user can set parameters. The program opens with an ‘action panel’, where the user can set an operating point (temperature, voltage, frequency, illumination), and an action list of calculations to carry out (I-V, C-V, C-f, Q(λ)). In each calculation, the running parameter (V, f or λ) is varied in the specified range, whilst all other parameters have the value specified in the operation point. Also, the user can directly view previously calculated results: I-V, C-V, C-f diagrams, electric field, carrier densities, partial recombination currents.

Like any numerical program, SCAPS solves the basic semiconductor equations. The basic equations are: the Poisson equation, relating the charge to the electrostatic potential \( \varphi \), and the continuity equations for electrons and holes. In one dimension, the total cell length \( L \) is divided in \( N \) intervals, and the value of \( \varphi_i \) and of the electron and hole concentrations \( n_i \) and \( p_i \) at each of the intervals constitute the unknowns of the problem. They can be found by numerically solving 3N non-linear equations, i.e. the basic equations at each of the intervals \( i \). Alternatively, one can choose \( \varphi_i \), \( n_i \) and \( p_i \) as independent variables instead of \( \varphi_i, n_i, p_i \). Here \( \phi_n \) and \( \phi_p \) are the quasi-fermi energy levels for electrons and holes respectively. The basic equations are non-linear because the continuity equations contain a recombination term, which is non-linear in \( n \) and \( p \).

The simplest model of charge transport that is useful is the Drift-Diffusion Model. This model is adequate for nearly all devices that were technologically feasible. This model is based on the two first equations cited above. The Poisson’s equation which relates the electrostatic potential to the space charge density:

\[
\text{div}(\varepsilon \nabla \varphi) = -\rho
\]  

(6)

where \( \varphi \) is the electrostatic potential, \( \varepsilon \) is the local permittivity, and \( \rho \) is the local space charge density. The continuity equations for electrons (for example) in steady state, is given by:

\[
0 = \frac{1}{q} \frac{d}{dt} j_n^+ + G_n - R_n
\]  

(7)

where \( n \) is the electron concentration, \( j_n^+ \) is the electron current density, \( G_n \) is the generation rate for electrons, \( R_n \) is the recombination rate for electrons, and \( q \) is the electron charge.

In the drift-diffusion model, the current density is expressed in terms of the quasi-Fermi level \( \phi_n \) as:

\[
j_n = -q \mu_n n \n \varphi_n
\]  

(8)

where \( \mu_n \) is the electron mobility. The quasi-Fermi level is then linked to the carrier concentration and the potential through the Boltzmann approximation:

\[
\phi_n = \psi - \frac{k_B T}{q} \ln \frac{n}{n_i}
\]  

(9)

where \( n_i \) is the effective intrinsic concentration and \( T \) is the lattice temperature. By substituting this equation
into the current density expression, the current is:

\[ J_n = q D_n \nabla n - q \mu_n n \nabla \psi - \mu_n n k_B T \nabla \ln(n_i) \] (10)

The final term accounts for the gradient in the effective intrinsic carrier concentration, which takes account of bandgap narrowing effects. The conventional formulation of drift-diffusion equation is:

\[ J_n = q D_n \nabla n + q \mu_n n \tilde{E}_n \] (11)

\[ \tilde{E}_n = -\nabla \psi - \frac{k_B T}{q} \nabla \ln(n_i) \] (12)

The electrical characteristics are calculated following the specified physical structure and bias conditions. This is achieved by approximating the operation of the device onto a one dimensional grid, consisting of a number of grid points called nodes. By applying the set of differential equations (Poisson's and continuity equations) onto this grid (discretization), the transport of carriers through the structure can be simulated. The finite element grid is used to represent the simulation domain.

The Si solar cell used in this work is similar to that of [33]. It is a typical 50 μm thick n+-p-p+ structure used for space applications. The different parameters of this solar cell are presented in Table 1.

<table>
<thead>
<tr>
<th>Thickness (μm)</th>
<th>Doping density (cm⁻³)</th>
<th>Type</th>
</tr>
</thead>
<tbody>
<tr>
<td>Emitter</td>
<td>0.15</td>
<td>1 x 10ⁱ⁹</td>
</tr>
<tr>
<td>Base</td>
<td>49.70</td>
<td>1 x 10ⁱ⁵</td>
</tr>
</tbody>
</table>
| Back surface field region | 0.15 | 5 x 10⁰⁸ | p⁺ |}

The I-V characteristics are calculated under AM0 for different fluences of 1 MeV electrons. Irradiation by these energetic creates defects in the Si lattice which manifest as recombination centres or traps for free carriers. A lot of work is carried to characterise these defects so that a huge number of defects are detected in Si. For simplicity we have used the most common observed defects [1, 17]. These are summarized in Table 2.

<table>
<thead>
<tr>
<th>Activation energy (eV)</th>
<th>Capture cross section, σ (cm²)</th>
<th>Introduction rate, k (cm⁻¹)</th>
<th>Trap type</th>
</tr>
</thead>
<tbody>
<tr>
<td>( E_V + 0.18 )</td>
<td>( 3.1 \times 10^{-15} )</td>
<td>0.002</td>
<td>Majority</td>
</tr>
<tr>
<td>( E_V + 0.36 )</td>
<td>( 6.2 \times 10^{-15} )</td>
<td>0.016</td>
<td>Majority</td>
</tr>
<tr>
<td>( E_C - 0.20 )</td>
<td>( 9.9 \times 10^{-15} )</td>
<td>0.002</td>
<td>Minority</td>
</tr>
<tr>
<td>( E_V + 0.56 )</td>
<td>( 6.3 \times 10^{-13} )</td>
<td>0.002</td>
<td>Majority</td>
</tr>
<tr>
<td>( E_C - 0.71 )</td>
<td>( 3.55 \times 10^{-13} )</td>
<td>0.004</td>
<td>Minority</td>
</tr>
</tbody>
</table>

3. Results and discussions

Since the solar cell used in this work has an n⁺-p-p⁺ structure, it is expected that the defects will be mainly created within the thickest region which is the p-type base. Therefore the majority traps will only contribute to the reduction of the minority carrier lifetime but not to the type inversion. It is therefore the minority traps which will be responsible for this phenomenon. Referring to table 2, there only two minority traps: \( E_C - 0.20 \) and \( E_C - 0.71 \). The second, the deepest, is only observed in type converted Si. In order to establish which trap is responsible for the type inversion we will calculate the I-V characteristics under the effect of each trap. Obviously, the majority traps are taken into account in both cases.

First when only the shallower trap, \( E_C - 0.20 \), is taken into account, the calculated I-V characteristics under different fluences are shown in Figure 1. It is clear that both the short circuit current and the open circuit voltage
decrease with increasing fluence of electron irradiation. However the fill factor (FF) does not change much. The extracted short circuit current normalized to the initial, non irradiated case, is presented in Figure 2.

![Figure 1](image1.png)

Figure 1. The calculated I-V characteristics of the n+-p-p+ Si solar cell under AM0 for different fluences of 1 MeV electron irradiation taking into account the majority traps and only the shallower minority trap, $E_C = 0.20$.

We can clearly see that the short circuit current decreases monolithically with increasing electron fluence. Therefore the shallower minority trap, $E_C = 0.20$, does not cause the type inversion of the p-type Si base.

![Figure 2](image2.png)

Figure 2. The extracted short circuit current, normalized to the unirradiated value, from the calculated I-V characteristics (Figure 1) of the n+-p-p+ Si solar cell under AM0 for different fluences of 1 MeV electron irradiation taking into account the majority traps and only the shallower minority trap, $E_C = 0.20$.

Next we will consider the effect deeper minority trap, $E_C = 0.71$, on the I-V characteristics of the n+-p-p+ Si solar cell under AM0 for different fluences of 1 MeV electron irradiation. When this trap is taken into account, the calculated I-V characteristics are completely different. These are presented in Figure 3.
Figure 3. The calculated I-V characteristics of the n+-p-p+ Si solar cell under AM0 for different fluences of 1 MeV electron irradiation taking into account all traps.

It is very clear the big difference from the I-V characteristics of Figure 1. There are two main differences. First the fill factor is hugely affected in contrast to the previous case. Second, the other figures of merit all decrease monolithically with increasing electron fluence except the short circuit current which decreases then increases at a certain fluence before it decreases again and abruptly. This is the type inversion case. To see this phenomenon even clearly, the short circuit current is extracted from the I-V characteristics. It is then normalized to the unirradiated value and presented in Figure 4.

Figure 4. The extracted short circuit current, normalized to the unirradiated value, from the calculated I-V characteristics (Figure 1) of the n+-p-p+ Si solar cell under AM0 for different fluences of 1 MeV electron irradiation taking into account all traps.

In this figure the type inversion phenomenon can be clearly seen. It is also worth to mention that the fluence at which this phenomenon appears is very comparable to measurements of [1, 17]. Although the shallower trap is closer to the conduction band it is less efficient for trapping electrons from the valence band. Therefore it is expected that it will have no effect on the free carrier density. On the other hand the deep minority trap is closed to the valence band therefore it can interchange electrons more easily with the valence band. Since it is a donor, it can give more electrons to the valence band and hence may change Si from p-type to n-type.
4. Conclusion

Numerical simulation using the software SCAPS was carried out to study the effect of 1 MeV electron irradiation of an n+-p-p+ Si solar cell under AM0. Irradiation induces structural defects in the Si lattice. These defects introduce energy levels in the Si forbidden energy gap and which act as recombination centres and/or traps of free carriers. The solar cell performance suffers a severe deterioration as a result. We have concentrated on the type inversion phenomenon which occurs at certain electron fluence. To elucidate this effect, the I-V characteristics where calculated taking into consideration the minority traps separately. It was concluded that the deeper minority trap is responsible for the type inversion phenomenon.

Acknowledgements

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References


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